## ME 3117 Heat Transfer

## Tutorial 1 - Introduction to Heat Transfer

(1) A heat rate of 3 kW is conducted through a section of an insulating material of cross-sectional area $10 \mathrm{~m}^{2}$ and thickness 2.5 cm . If the inner (hot) surface temperature is $415^{\circ} \mathrm{C}$ and the thermal conductivity of the material is $0.2 \mathrm{~W} / \mathrm{m} . \mathrm{K}$, what is the outer surface temperature? (Answer: $378{ }^{\circ} \mathrm{C}$ )
(2) The inner and outer surface temperatures of a glass window 5 mm thick are 15 and 5C. What is the heat loss thorough a window that is 1 m and 3 m on a side. The thermal conductivity of glass is $1.4 \mathrm{~W} / \mathrm{m} . \mathrm{K}$. (Answer: 8400 W )
(3) A freezer compartment consists of a cubical cavity that is 2 m on a side. Assume the bottom to be perfectly insulated. What is the minimum thickness of styrofoam insulation ( $\mathrm{k}=0.030 \mathrm{~W} / \mathrm{m} . \mathrm{K}$ ) that must be applies to the top and side walls to ensure a heat load of less than 500 W , when the inner and outer surface are $-10^{\circ} \mathrm{C}$ and $35^{\circ} \mathrm{C}$ ? (Answer: $54 \mathbf{m m}$ )
(4) An electric resistance heater is embedded in a long cylinder of diameter 30 mm . When water with a temperature of $25^{\circ} \mathrm{C}$ and velocity of $1 \mathrm{~m} / \mathrm{s}$ flows crosswise over the cylinder, the power per unit length required to maintain the surface at a uniform temperature of $90^{\circ} \mathrm{C}$ is $28 \mathrm{~kW} / \mathrm{m}$. When air, also at $25^{\circ} \mathrm{C}$, but velocity of $10 \mathrm{~m} / \mathrm{s}$ is flowing, the power per unit length required to maintain the same surface temperature is $400 \mathrm{~W} / \mathrm{m}$. Calculate and compare the convection coefficients for the flows of water and air. (Answer: $\mathbf{4 5 7 0} \mathbf{W} / \boldsymbol{m}^{2} . \boldsymbol{K}, \mathbf{6 5} \mathbf{W} / \boldsymbol{m}^{2}$. K)
(5) A square isothermal chip is of width $w=5 \mathrm{~mm}$ on a side and is mounted in a substrate such that its side and back surfaces are well insulated, while the front surface is exposed to the flow of a coolant at $\mathrm{T}_{\infty}=15^{\circ} \mathrm{C}$. From reliability considerations, the chip temperature must not exceed $\mathrm{T}=85^{\circ} \mathrm{C}$. If the coolant is air and the corresponding coefficient is $\mathrm{h}=200 \mathrm{~W} / \mathrm{m}^{2} . \mathrm{K}$, what is the maximum allowable chip power? If the coolant is a dielectric liquid for which $\mathrm{h}=3000$ $\mathrm{W} / \mathrm{m} 2 . \mathrm{K}$, what is the maximum allowable power? (Answer: 0.35W, 5.25 W)
(6) A surface of area $0.5 \mathrm{~m}^{2}$, emissivity 0.8 , and temperature $150^{\circ} \mathrm{C}$ is place in a large, evacuated chamber whose walls are maintained at $25^{\circ} \mathrm{C}$. What is the rate at which radiation is emitted by the surface? What is the net rate at which radiation is exchanged between the surface and the chamber walls? (Answer: 726 W, 547 W)

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Tutorial 2a-Conduction
(1) Assume steady-state, one-dimensional heat conduction through the axisymmetric shape shown on the right. Assume constant properties and no internal heat generation, sketch the temperature distribution on T-x coordinates.

(2) A hot water pipe with outside radius $r_{1}$ has a temperature $T_{1}$. A thick insulation applied to reduce the heat loss has an outer radius $\mathrm{r}_{2}$ and temperature $\mathrm{T}_{2}$. On T-r coordinates, sketch the temperature distribution in the insulation for onedimentional, steady-state heat transfer with constant properties.
(3) Assume steady-state, one-dimensional heat conduction through the symmetric shape shown. Assuming that there is no internal heat generation, derive an expression for the thermal conductivity $k(x)$ for these conditions: $A(x)=(1-x)$, $T(x)=300\left(1-2 x-x^{3}\right)$, and $q=6000 W$, where A is in square meters, $T$ in Kelvin, and $x$ in meters.

(4) One dimensional, steady-state conduction without heat generation occurs in the system shown. The thermal conductivity is $25 \mathrm{~W} / \mathrm{m} . \mathrm{K}$ and the thickness L is 0.5 m . Determine the unknown quantities for each case in the accompanying table and sketch the temperature distribution, indicating the direction of the heat flux.


| Case | $\mathrm{T}_{1}$ | $\mathrm{~T}_{2}$ | $\mathrm{dT} / \mathrm{dx}$ <br> $(\mathrm{K} / \mathrm{m})$ | $\mathrm{q} "{ }_{\mathrm{x}}$ <br> $\left(\mathrm{W} / \mathrm{m}^{2}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 400 K | 300 K |  |  |
| 2 | $100^{\circ} \mathrm{C}$ |  | -250 |  |
| 3 | $80^{\circ} \mathrm{C}$ |  | 200 |  |
| 4 |  | $-5{ }^{\circ} \mathrm{C}$ |  |  |
| 5 | $30^{\circ} \mathrm{C}$ |  |  |  |

(5) Consider a plane wall 100 mm thick and of thermal conductivity $100 \mathrm{~W} / \mathrm{m} . \mathrm{K}$. Steady-state conditions are known to exist with $\mathrm{T} 1=400 \mathrm{~K}$ and $\mathrm{T} 2=600 \mathrm{~K}$. Determine the heat flux and the temperature gradient for the coordinate systems shown.

(6) A cylinder of radius $r_{0}$, length $L$, and thermal conductivity $k$ is immersed in a fluid of convection coefficient $h$ and unknown temperature $\mathrm{T}_{\infty}$. At a certain instant the temperature distribution in the cylinder is $\mathrm{T}(\mathrm{r})=\mathrm{a}+\mathrm{br}^{2}$, where $a$ and $b$ are constants. Obtain expressions for the heat transfer rate at the fluid temperature.

