- (1) A heat rate of 3 kW is conducted through a section of an insulating material of cross-sectional area 10 m<sup>2</sup> and thickness 2.5 cm. If the inner (hot) surface temperature is 415°C and the thermal conductivity of the material is 0.2 W/m.K, what is the outer surface temperature? (Answer: 378 °C)
- (2) The inner and outer surface temperatures of a glass window 5 mm thick are 15 and 5C. What is the heat loss thorough a window that is 1 m and 3 m on a side. The thermal conductivity of glass is 1.4 W/m.K. (Answer: 8400 W)
- (3) A freezer compartment consists of a cubical cavity that is 2 m on a side. Assume the bottom to be perfectly insulated. What is the minimum thickness of styrofoam insulation (k = 0.030 W/m.K) that must be applies to the top and side walls to ensure a heat load of less than 500 W, when the inner and outer surface are -10°C and 35 °C? (*Answer: 54 mm*)
- (4) An electric resistance heater is embedded in a long cylinder of diameter 30 mm. When water with a temperature of 25 °C and velocity of 1 m/s flows crosswise over the cylinder, the power per unit length required to maintain the surface at a uniform temperature of 90°C is 28 kW/m. When air, also at 25°C, but velocity of 10 m/s is flowing, the power per unit length required to maintain the same surface temperature is 400 W/m. Calculate and compare the convection coefficients for the flows of water and air. (Answer: 4570 W/m<sup>2</sup>.K, 65 W/m<sup>2</sup>.K)
- (5) A square isothermal chip is of width w = 5mm on a side and is mounted in a substrate such that its side and back surfaces are well insulated, while the front surface is exposed to the flow of a coolant at  $T_{\infty}$  =15°C. From reliability considerations, the chip temperature must not exceed T = 85°C. If the coolant is air and the corresponding coefficient is h = 200 W/m<sup>2</sup>.K, what is the maximum allowable chip power? If the coolant is a dielectric liquid for which h = 3000 W/m<sup>2</sup>.K, what is the maximum allowable power? (*Answer: 0.35W, 5.25 W*)
- (6) A surface of area  $0.5 \text{ m}^2$ , emissivity 0.8, and temperature 150°C is place in a large, evacuated chamber whose walls are maintained at 25°C. What is the rate at which radiation is emitted by the surface? What is the net rate at which radiation is exchanged between the surface and the chamber walls? (*Answer: 726 W, 547 W*)

## ME 3117 Heat Transfer Tutorial 2a – Conduction

(1) Assume steady-state, one-dimensional heat conduction through the axisymmetric shape shown on the right. Assume constant properties and no internal heat generation, sketch the temperature distribution on T-x coordinates.



- (2) A hot water pipe with outside radius r<sub>1</sub> has a temperature T<sub>1</sub>. A thick insulation applied to reduce the heat loss has an outer radius r<sub>2</sub> and temperature T<sub>2</sub>. On T-r coordinates, sketch the temperature distribution in the insulation for one-dimensional, steady-state heat transfer with constant properties.
- (3) Assume steady-state, one-dimensional heat conduction through the symmetric shape shown. Assuming that there is no internal heat generation, derive an expression for the thermal conductivity k(x) for these conditions: A(x) = (1-x),  $T(x) = 300(1 2x x^3)$ , and q = 6000 W, where A is in square meters, T in Kelvin, and x in meters.



(4) One dimensional, steady-state conduction without heat generation occurs in the system shown. The thermal conductivity is 25 W/m.K and the thickness L is 0.5m. Determine the unknown quantities for each case in the accompanying table and sketch the temperature distribution, indicating the direction of the heat flux.



(5) Consider a plane wall 100 mm thick and of thermal conductivity 100 W/m.K. Steady-state conditions are known to exist with T1 = 400 K and T2 = 600 K. Determine the heat flux and the temperature gradient for the coordinate systems shown.



(6) A cylinder of radius  $r_0$ , length L, and thermal conductivity k is immersed in a fluid of convection coefficient h and unknown temperature  $T_{\infty}$ . At a certain instant the temperature distribution in the cylinder is  $T(r) = a + br^2$ , where a and b are constants. Obtain expressions for the heat transfer rate at the fluid temperature.